

$$\frac{da}{dN} = 3.68 \times 10^{-12} (\Delta K_{IC})^4$$



$$K_{IC} = 80 \text{ MPa}\sqrt{\text{m}}$$

$$\sigma_{\max} = 403 \text{ MPa}$$

$$a_0 = 2 \text{ mm}$$

$$\Delta\sigma = 403 \text{ MPa}$$

$$a_f = 10 \text{ mm}$$

$$n = 4$$

$$R = 0$$

$$\Rightarrow K_{IC} = f(a/w) \sigma_{\max} \sqrt{\pi a_f}$$

$$\Rightarrow \frac{da}{dN} = 3.68 \times 10^{-12} (f(a/w) \Delta\sigma \sqrt{\pi a_f})^4$$

$$\Rightarrow \int_{a_0}^{a_f} \frac{da}{a^2} = 3.68 \times 10^{-12} \times (f(a/w) \Delta\sigma \sqrt{\pi a_f})^4 \int_0^{N_f} dN$$

$$\Rightarrow \left. \frac{-1}{a} \right|_{a_0}^{a_f} = 3.68 \times 10^{-12} \left(1.12 \times 403 \times 10^{-6} \sqrt{\pi \times 10 \times 10^{-3}} \right)^4 \int_0^{N_f} dN$$

$$\Rightarrow a_0^{-1} - a_f^{-1} = 1.51 N_f \Rightarrow N_f = 278.3 \text{ cycl}$$

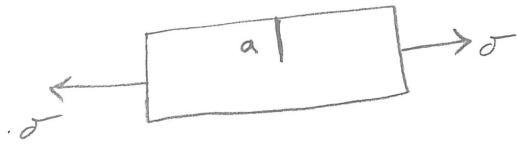
$$t = \frac{N_f}{f} = \frac{278.3}{0.02} = 13916 \text{ sec} = 3.87 \text{ hour}$$

$$\frac{da}{dN} = 2 \times 10^{-8} (\Delta K_{IC})^{2.45} = 2 \times 10^{-8} (1.12 \Delta\sigma \sqrt{\pi a})^{2.45} \quad (2)$$

$$\int_{a_0}^{a_f} \frac{da}{a^{2.45}} = 0.1257 \int_0^{N_f} dN = 4732.3 \Rightarrow \frac{a_0^{-1.45} - a_c^{-1.45}}{1.45} = 4732.3$$

$$\Rightarrow a_c = a_f = 7 \text{ mm}$$

$$K_{IC} = 1.12 \Delta\sigma \sqrt{\pi a_c} = 1.12 \times 300 \sqrt{\pi \times 7 \times 10^{-3}} = 50 \text{ MPa}\sqrt{\text{m}}$$



a) $a = 7.86 \times 10^{-8} \text{ m}$

$\left. \frac{da}{dN} \right|_a = \frac{\Delta a}{\Delta N} = 7.86 \times 10^{-8}$

$\Delta K = E \sqrt{\frac{a}{6}}$ $E \text{ (MPa)}$ $\Rightarrow \Delta K = 207 \times 10^3 \sqrt{\frac{7.86 \times 10^{-8}}{6}} = 23.69 \text{ MPa}\sqrt{\text{m}}$
 $a \text{ (m)}$

$\Rightarrow \Delta \sigma = \frac{\Delta K}{\sqrt{\pi a}} = \frac{23.69 \text{ MPa}\sqrt{\text{m}}}{\sqrt{\pi(0.01 \text{ m})}} = 133.66 \text{ MPa} = \sigma_{\text{max}}$

b) $\Delta K_b = \Delta \sigma \sqrt{\pi a} = (133.66) \sqrt{\pi(0.02)} = 33.5 \text{ MPa}\sqrt{\text{m}}$

$a = 6 \left(\frac{\Delta K}{E} \right)^2 = 6 \left(\frac{33.5 \text{ MPa}\sqrt{\text{m}}}{207 \times 10^3 \text{ MPa}} \right)^2 = 1.57 \times 10^{-7} \text{ m}$

$\frac{da}{dN} = \frac{\Delta a}{\Delta N} = \frac{a}{\Delta N} = 1.57 \times 10^{-7} \text{ m/cycle}$

c) $\left. \frac{da}{dN} \right|_a = A (\Delta K_a)^n$ $\Rightarrow n = \frac{\ln \left[\frac{\left. \frac{da}{dN} \right|_a}{\left. \frac{da}{dN} \right|_b} \right]}{\ln \left(\frac{\Delta K_a}{\Delta K_b} \right)} = \frac{\ln \left(\frac{7.86 \times 10^{-8}}{1.57 \times 10^{-7}} \right)}{\ln \left(\frac{23.69}{33.5} \right)} = 2$

$\left. \frac{da}{dN} \right|_b = A (\Delta K_b)^n$

$\Rightarrow A = \frac{\left(\frac{da}{dN} \right)_a}{(\Delta K_a)^n} = \frac{7.86 \times 10^{-8}}{(23.69)^2} = 1.4 \times 10^{-10}$ $\Rightarrow \left. \frac{da}{dN} \right|_{\sigma, b} = 1.4 \times 10^{-10} (\Delta K)^2$

d) $K_{Ic} = \sigma_{\text{max}} \sqrt{\pi a_c} = (133.66) \sqrt{\pi(0.03)} = 41 \text{ MPa}\sqrt{\text{m}}$